

## FACULTY OF COMMERCE, HUMAN SCIENCES AND EDUCATION

# DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

| QUALIFICATION: BACHELOR OF ECONOMICS HONOURS DEGREE |             |            |                                   |  |  |
|---|-------------|------------|-----------------------------------|--|--|
| QUALIFICATION CO                                    | DDE: 08HECO | LEVEL:     | 8                                 |  |  |
| COURSE CODE:  | AEM810S     | COURSE NAM | COURSE NAME: APPLIED ECONOMETRICS |  |  |
| SESSION:  |             | PAPER:     | THEORY                            |  |  |
| DURATION:   | 3 HOURS     | MARKS:     | 100                               |  |  |

| SECOND OPPORTUNITY QUESTION PAPER |                         |  |  |
|-----------------------------------|-------------------------|--|--|
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| MODERATOR:                        | Dr. Reinhold Kamati     |  |  |

| INSTRUCTIONS |    |                           |
|--------------|----|---------------------------|
|              | 1. | Answer all questions.     |
|              | 2. | Write clearly and neatly. |
|              | 3. | Number the answers.       |

## PERMISSIBLE MATERIALS

- 1. Ruler
- 2. calculator

THIS QUESTION PAPER CONSISTS OF 6 PAGES

QUESTION 1 [25 marks]

- a) State the formulae used to test for unit roots using the Dickey Fuller test and the Augmented Dickey Fuller test. [12]
- b) What is the difference between the two tests? [2]
- c) State the hypotheses and the decision rules for the tests in (a).[3]
- d) What orders of integration are appropriate when using the methods in Table 1? [8]

#### Table 1

| Me  | thodology | Appropriate order of integration |
|-----|-----------|----------------------------------|
| i.  | OLS       |                                  |
| ii. | ECM       |                                  |
| ii. | ARDL      |                                  |
| iv. | ARDL-ECM  |                                  |
| v.  | VAR       |                                  |
| vi. | VECM      |                                  |

#### QUESTION 2 [25 marks]

Explain all steps you would take to apply the cointegration and error correction modelling (ECM) technique. Assume that the dependent variable is Gross Domestic Product (Y), and the independent variables are Capital (K) and Labour (L).

- a) What order of integration of the variables is appropriate to run this model?
- b) Specify the long-run equation with an intercept and no trend. [5]
- c) Explain how you generate the errors and use them to test for cointegration (state the hypothesis and decision rule for the cointegration test).
- d) If there is no cointegration, what do you do? [2]
- e) If there is cointegration among the variables, state the model you estimate. [5]

f) Which parameters in your model are short-run and which parameters are long-run? [5]

#### QUESTION 3 [25 marks]

(a) Suppose you want to test for the Dynamic Granger causality between GDP (Y) and money supply (M), whose model is given as follows:

$$\Delta Y_{t} = \lambda_{0} + \sum_{i=1}^{n} \lambda_{1i} \Delta Y_{t-i} + \sum_{i=1}^{n} \lambda_{2i} \Delta M_{t-1} + \lambda_{3} \epsilon_{1t-1} + \mu_{1t}$$
 (1)

$$\Delta M_t = \varphi_0 + \sum_{i=1}^n \varphi_{1i} \Delta Y_{t-i} + \sum_{i=1}^n \varphi_{2i} \Delta M_{t-1} + \varphi_3 \epsilon_{2t-1} + \mu_{2t}$$
 (2)

- a) State the hypothesis and decision rule used when testing whether money supply Granger causes GDP. [5]
- b) State the hypothesis and decision rule used when testing whether GDP Granger causes Money Supply. [5]
- c) State the joint Granger causality hypotheses for the two equations. [5]
- d) State the conditions that must be met in this VAR model to have feedback causality. [5]
- e) State the conditions that must be met in this VAR model to have unidirectional causality running from M to Y. [5]

# QUESTION 4 [25 marks]

Use the estimated model below in Table 1 to answer the following questions:

- a) State the econometrics method used to obtain these results? [1]
- b) What is the order of integration of the variables used in the model? [1]
- c) Is the estimated model over-parameterized or parsimonious? [1]
- d) Interpret the DW statistic in each of the estimated models? [3]
- e) Comment on all the possible Granger causality relationships you observe in the results. [7]

Table 1

System: UNTITLED

Estimation Method: Least Squares
Date: 06/03/21 Time: 15:55
Sample: 1993 2019
Included observations: 27

| included observation                            | 15. 41                                  |                    |                      |            |
|---|---|--------------------|----------------------|------------|
| Total system (balance                           | ed) observations                        | s 81               |                      |            |
|   | Coefficient                             | Std. Error         | t-Statistic          | Prob.      |
| C(2)  | -0.847813                               | 0.299441           | -2.831313            | 0.0061     |
| C(3)  | 0.610685                                | 0.192159           | 3.178019             | 0.0022     |
| C(6) 0.132214                                   |   | 0.065553           | 2.016896             | 0.0476     |
| C(7)  | 0.030303                                | 0.008845           | 3.425799             | 0.0010     |
| C(9)  | -1.006227                               | 0.217585           | -4.624524            | 0.0000     |
| C(10)   | 0.480942                                | 0.139630           | 3.444412             | 0.0010     |
| C(13)   | 0.171119                                | 0.047633           | 3.592429             | 0.0006     |
| C(14)   | 0.039613                                | 0.006427           | 6.163073             | 0.0000     |
| C(16)   | -3.543975                               | 1.070876           | -3.309417            | 0.0015     |
| C(17)   | 4.801334                                | 0.906802           | 5.294798             | 0.0000     |
| C(19)   | -0.474299                               | 0.186298           | -2.545917            | 0.0131     |
| C(20)   | 0.350457                                | 0.256055           | 1.368676             | 0.1755     |
| 0(20)   | 0.000107                                | 0.20000            | 1.000070             | 0.1700     |
| Determinant residua                             | l covariance                            | 2.65E-11           |                      |            |
| Equation: D(LNGDP) = C(2)                       | *D(LNGDP(-2)) + C(3)                    | *D(LNPCE(-1)) + C  | 2(6) *D(LNPDI(-2)) - | + C(7)     |
|   |   |                    |                      |            |
| Observations: 27                                |   |                    |                      |            |
| R-squared                                       | 0.404463                                | Mean depende       |                      | 0.029535   |
| Adjusted R-squared                              | 0.326784                                | S.D. depender      |                      | 0.021068   |
| S.E. of regression                              | 0.017286                                | Sum squared resid  |                      | 0.006873   |
| Durbin-Watson stat                              | 2.431954                                |                    |                      |            |
| Equation, D(I NDOE) - Q(0)                      | *D(I NODD( 0)) + 0(10                   | )+D/I NDOE/ 1)) +  | O(12)*D(1 NDD1/ O    | N + O(14)  |
| Equation: $D(LNPCE) = C(9)^{-1}$                | "D(LNGDP(-2)) + C(10                    | )^D(LNPCE(-1)) +   | C(13)*D(LNPDI(-2)    | )) + C(14) |
| Observations: 27                                | 200111111111111111111111111111111111111 |                    |                      |            |
| R-squared                                       | 0.553562                                | Mean depende       | 0.031553             |            |
| Adjusted R-squared                              | 0.495331                                | S.D. dependent var |                      | 0.017681   |
| S.E. of regression                              | 0.012561                                | Sum squared resid  |                      | 0.003629   |
| Durbin-Watson stat                              | 2.008833                                |                    |                      |            |
|   |   |                    |                      |            |
| Equation: D(LNPDI) = C(16<br>C(20)*D(LNPDI(-2)) | 5)*D(LNGDP(-2)) + C(1                   | 7)*D(LNPCE(-1)) -  | + C(19)*D(LNPDI(-1   | .)) +      |
| Observations: 27                                |   |                    |                      |            |
| R-squared                                       | 0.512427                                | Mean depende       | ent var              | 0.041603   |
| Adjusted R-squared                              | 0.448831                                | S.D. depender      |                      | 0.102684   |
| S.E. of regression                              | 0.076234                                | Sum squared        |                      | 0.133666   |
| Durbin-Watson stat                              | 2.332224                                |                    |                      |            |
|   |   |                    |                      |            |

#### f) Explain how you get the lag length from these results.

[6]

Table 2: VAR Lag Order Selection Criteria

Endogenous variables: D(LNGDP) D(LNPCE) D(LNPDI)

Exogenous variables: C

Date: 06/03/21 Time: 16:36

Sample: 1990 2019 Included observations: 27

| Lag | LogL     | LR        | FPE      | AIC        | SC         | HQ         |
|-----|----------|-----------|----------|------------|------------|------------|
| 0   | 201.9214 | NA        | 8.00e-11 | -14.73492  | -14.59094* | -14.69211  |
| 1   | 207.0165 | 8.680476  | 0.108    | -14.44566  | -13.86974  | -14.27441  |
| 2   | 229.7969 | 33.74871* | 0.00399  | -15.46643* | -14.45856  | -15.16674* |

<sup>\*</sup> indicates lag order selected by the criterion

LR: sequential modified LR test statistic (each test at 5% level)

FPE: Final prediction error

AIC: Akaike information criterion SC: Schwarz information criterion

HQ: Hannan-Quinn information criterion

## g) Interpret the cointegrating results below.

[6]

Table 3: Unrestricted Cointegration Rank Test (Trace)

| Hypothesized<br>No. of CE(s) | Eigenvalue | Trace<br>Statistic | 0.05<br>Critical Value | Prob.** |
|------------------------------|------------|--------------------|------------------------|---------|
| None *                       | 0.873210   | 61.18868           | 29.79707               | 0.0000  |
| At most 1                    | 0.147946   | 5.427621           | 15.49471               | 0.7619  |
| At most 2                    | 0.040092   | 1.104782           | 3.841465               | 0.2932  |

Trace test indicates 1 cointegrating eqn(s) at the 0.05 level

#### Unrestricted Cointegration Rank Test (Maximum Eigenvalue)

| Hypothesized<br>No. of CE(s) | Eigenvalue | Max-Eigen<br>Statistic | 0.05<br>Critical Value | Prob.** |
|------------------------------|------------|------------------------|------------------------|---------|
| None * At most 1 At most 2   | 0.873210   | 55.76106               | 21.13162               | 0.0000  |
|                              | 0.147946   | 4.322839               | 14.26460               | 0.8238  |
|                              | 0.040092   | 1.104782               | 3.841465               | 0.2932  |

Max-eigenvalue test indicates 1 cointegrating eqn(s) at the 0.05 level

<sup>\*</sup> Denotes rejection of the hypothesis at the 0.05 level

<sup>\*\*</sup>MacKinnon-Haug-Michelis (1999) p-values

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